

**2024
VCE
Mathematical Methods
Year 12
Trial Examination 2
Detailed Answers**



Kilbaha Education

Quality educational content

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SECTION A

ANSWERS

| | | | | |
|-----------|----------|----------|----------|----------|
| 1 | A | B | C | D |
| 2 | A | B | C | D |
| 3 | A | B | C | D |
| 4 | A | B | C | D |
| 5 | A | B | C | D |
| 6 | A | B | C | D |
| 7 | A | B | C | D |
| 8 | A | B | C | D |
| 9 | A | B | C | D |
| 10 | A | B | C | D |
| 11 | A | B | C | D |
| 12 | A | B | C | D |
| 13 | A | B | C | D |
| 14 | A | B | C | D |
| 15 | A | B | C | D |
| 16 | A | B | C | D |
| 17 | A | B | C | D |
| 18 | A | B | C | D |
| 19 | A | B | C | D |
| 20 | A | B | C | D |

SECTION A

Question 1

Answer A

Both functions have periods $T = \frac{2\pi}{\frac{\pi}{c}} = 2c$, both functions have an amplitude of b ,

both functions have a range of $[a-b, a+b]$

Question 2

Answer C

$f(x) = \log_e(b-x)$ domain $b-x > 0$, $x < b$

$g(x) = \sqrt{x+b}$ domain $x+b \geq 0$, $x \geq -b$,

domain of $\frac{f}{g} = -b < x < b = (-b, b)$ since $g(x) \neq 0$

Define $f(x) = \ln(b-x)$ *Done*

Define $g(x) = \sqrt{x+b}$ *Done*

domain $\left(\frac{f(x)}{g(x)}, x\right)$ $-b < x < b$

Question 3

Answer A

$$\int_0^{4a} f(x) dx$$

$$= \int_0^{2a} f(x) dx + \int_{2a}^{4a} f(x) dx$$

$$= \int_0^{2a} f(x) dx - \int_{4a}^{2a} f(x) dx$$

$$= \int_0^{2a} f(x) dx - \int_{4a}^{2a} f(u) du \quad \text{let } u = 4a - x$$

$$= \int_0^{2a} f(x) dx + \int_0^{2a} f(4a-x) dx = \int_0^{2a} (f(x) + f(4a-x)) dx$$

Define $f(x) = x^3$ *Done*

$$\int_0^{4 \cdot a} f(x) dx = 64 \cdot a^4$$

$$\int_0^{2 \cdot a} (f(x) + f(4 \cdot a - x)) dx = 64 \cdot a^4$$

reflect in the y-axis

and translate $4a$ units to the right

Question 4

Answer B

| | | | | |
|----------------------|---|---------------|---------------|---------------|
| x | 1 | 2 | 3 | 4 |
| $f(x) = \frac{1}{x}$ | 1 | $\frac{1}{2}$ | $\frac{1}{3}$ | $\frac{1}{4}$ |

$$a = 1, \quad b = 4, \quad n = 3. \quad h = \frac{b-a}{n} = 1$$

$$A_T = \frac{h}{2} (f(1) + 2(f(2) + f(3)) + f(4)) = \frac{1}{2} \left(1 + 2 \left(\frac{1}{2} + \frac{1}{3} \right) + \frac{1}{4} \right) = \frac{35}{24}$$

Question 5 **Answer C**

Consider the function $f: R \rightarrow R$, $f(x) = x + 2$.

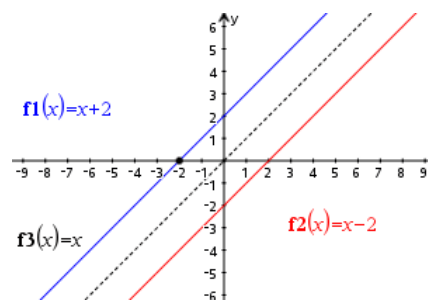
$$f: y = x + 2$$

$$f^{-1}: x = y + 2$$

$$f^{-1}(x) = x - 2$$

$$f(x) = f^{-1}(x) \Rightarrow x + 2 = x - 2$$

This equation is inconsistent, there is no solution, with $y = x$ as all three lines are parallel. Colin is correct.



Consider the function $f: R \rightarrow R$, $f(x) = -x^3$.

$$f: y = -x^3$$

$$f^{-1}: x = -y^3, y = -x^{\frac{1}{3}} = -\sqrt[3]{x}$$

both the function f and its inverse have domain and range R .

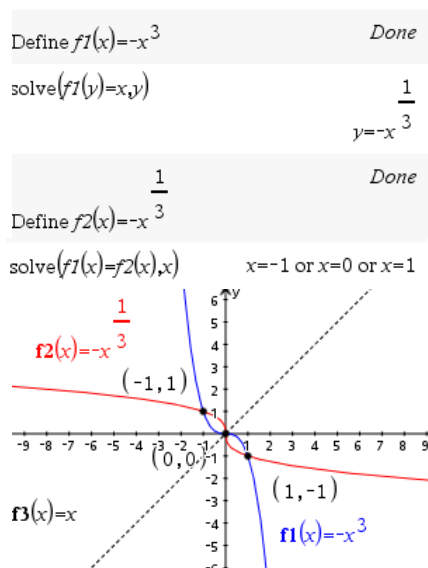
$$\text{solving } f(x) = f^{-1}(x) \Rightarrow (1) \quad -x^3 = -\sqrt[3]{x}$$

$$(1) \quad x^9 = x \Rightarrow x = 0, \pm 1$$

There are three points of intersection between the function and its inverse, with coordinates $(-1, 1)$, $(1, -1)$ and the origin $(0, 0)$. Only the point at the origin only lies on the line $y = x$.

Ben is correct.

Other functions are possible to show that both Ben and Colin are correct.



Question 6 **Answer B**

BR or RB, 2 ways of drawing one red and one blue, without replacement

$$\text{Box A: } \frac{1}{2} \left[\frac{(r-1)(b+1)}{(b+r)(b+r-1)} + \frac{(b+1)(r-1)}{(b+r)(b+r-1)} \right] = \frac{(r-1)(b+1)}{(b+r)(b+r-1)}$$

$$\text{Box B: } \frac{1}{2} \left[\frac{(r+1)(b-1)}{(b+r)(b+r-1)} + \frac{(b-1)(r+1)}{(b+r)(b+r-1)} \right] = \frac{(r+1)(b-1)}{(b+r)(b+r-1)}$$

$$\text{Box A or B } \frac{(r-1)(b+1)}{(b+r)(b+r-1)} + \frac{(r+1)(b-1)}{(b+r)(b+r-1)} = \frac{2(br-1)}{(b+r)(b+r-1)}$$

$$\frac{(r-1) \cdot (b+1) + (r+1) \cdot (b-1)}{(b+r) \cdot (b+r-1)} = \frac{2 \cdot (b \cdot r - 1)}{(b+r) \cdot (b+r-1)}$$

Question 7 **Answer D**

When $n = 2$, $y = \sqrt{x-a}$, $\frac{dy}{dx} = \frac{1}{2\sqrt{x-a}}$

When $n = -3$,

$$y = \frac{1}{\sqrt[3]{x-a}} = (x-a)^{-\frac{1}{3}}, \quad \frac{dy}{dx} = -\frac{1}{3}(x-a)^{-\frac{4}{3}}$$

When $n = -\frac{1}{2}$, $y = \frac{1}{(x-a)^2}$, $\frac{dy}{dx} = -\frac{2}{(x-a)^3}$

All of **A**, **B** and **C** are not differentiable at $x = a$.

When $n = \frac{1}{2}$, $y = (x-a)^2$ is differentiable at $x = a$

| | |
|---------------------------------|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=2$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | undef |

| | |
|----------------------------------|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=-3$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | undef |

| | |
|--|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=-\frac{1}{2}$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | undef |

| | |
|---|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=\frac{1}{2}$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | 0 |

| | |
|---|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=\frac{1}{2}$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | 0 |

| | |
|---|-------------|
| $\frac{1}{n}$ | <i>Done</i> |
| Define $f(x) = (x-a)^n$ $n=\frac{1}{2}$ | |
| $\frac{d}{dx}(f(x)) _{x=a}$ | 0 |

Question 8 **Answer A**

$$y = 4 \tan\left(2\left(x - \frac{\pi}{3}\right)\right) = \frac{4 \sin\left(2\left(x - \frac{\pi}{3}\right)\right)}{\cos\left(2\left(x - \frac{\pi}{3}\right)\right)}$$

crosses the x -axis when $y = 0$ so $\sin\left(2\left(x - \frac{\pi}{3}\right)\right) = 0$

has vertical asymptotes when $\cos\left(2\left(x - \frac{\pi}{3}\right)\right) = 0$

| | | | |
|--|--|---|---|
| solve $\left(\sin\left(2\left(x - \frac{\pi}{3}\right)\right) = 0, x\right)$ | $x = \frac{(3 \cdot n1 - 1) \cdot \pi}{6}$ | $x = \frac{(3 \cdot (k+1) - 1) \cdot \pi}{6}$ | $x = \frac{(3 \cdot k + 2) \cdot \pi}{6}$ |
|--|--|---|---|

| | | | |
|--|---|--|---|
| solve $\left(\cos\left(2\left(x - \frac{\pi}{3}\right)\right) = 0, x\right)$ | $x = \frac{(6 \cdot n2 - 5) \cdot \pi}{12}$ | $x = \frac{(6 \cdot (k-1) - 5) \cdot \pi}{12}$ | $x = \frac{(6 \cdot k - 11) \cdot \pi}{12}$ |
|--|---|--|---|

Question 9 **Answer C**

$$\Pr(X \geq 2) = 1 - [\Pr(X = 1) + \Pr(X = 0)] = 1 - \left[\binom{10}{1} 0.37 \times 0.63^9 + 0.63^{10} \right]$$

$n = 10$, $q = 0.63$, $p = 0.37$, at least two successes in ten trials each with a probability of 0.37

Question 10 **Answer A**

$$\left(\hat{p} - z\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}, \hat{p} + z\sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \right)$$

$$z_{95} = \text{invNorm}(0.975, 0, 1) \quad 1.9600$$

$$z_{99} = \text{invNorm}(0.995, 0, 1) \quad 2.5758$$

$$CI: 99\%, z = 2.5758 \quad \left(\hat{p} - 2.5758\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}, \hat{p} + 2.5758\sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \right) = (a, b)$$

$$(1) a = \hat{p} - 2.5758\sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \quad (2) b = \hat{p} + 2.5758\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$\frac{1}{2}((1)+(2)) \quad \hat{p} = \frac{a+b}{2}, \quad \frac{1}{2}((2)-(1)) \quad \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = \frac{b-a}{2 \times 2.5758}$$

CI: 95%, $z = 1.96$

$$\left(\hat{p} - 1.96\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}, \hat{p} + 1.96\sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \right)$$

$$\left(\frac{a+b}{2} - \frac{1.96(b-a)}{2 \times 2.5758}, \frac{a+b}{2} + \frac{1.96(b-a)}{2 \times 2.5758} \right)$$

$$\left(\frac{a}{2} \left(1 + \frac{1.96}{2.5758} \right) + \frac{b}{2} \left(1 - \frac{1.96}{2.5758} \right), \frac{a}{2} \left(1 - \frac{1.96}{2.5758} \right) + \frac{b}{2} \left(1 + \frac{1.96}{2.5758} \right) \right)$$

$$(0.88a + 0.12b, 0.12a + 0.88b)$$

| | | |
|--|----------|---------------------|
| zInterval_1Prop 20,100,0.99: <i>stat.results</i> | "Title" | "1-Prop z Interval" |
| | "CLower" | 0.097 |
| | "CUpper" | 0.303 |
| | "p" | 0.200 |
| | "ME" | 0.103 |
| | "n" | 100.000 |

$$0.88 \cdot \text{stat.CLower} + 0.12 \cdot \text{stat.CUpper} \quad 0.122$$

$$0.12 \cdot \text{stat.CLower} + 0.88 \cdot \text{stat.CUpper} \quad 0.278$$

| | | |
|--|----------|---------------------|
| zInterval_1Prop 20,100,0.95: <i>stat.results</i> | "Title" | "1-Prop z Interval" |
| | "CLower" | 0.122 |
| | "CUpper" | 0.278 |
| | "p" | 0.200 |
| | "ME" | 0.078 |
| | "n" | 100.000 |

Question 11 **Answer D**

$$f(x) = g(x)e^{g(x)} \quad \text{using the product rule}$$

$$f'(x) = \frac{d}{dx}(g(x)) \times e^{g(x)} + g(x) \frac{d}{dx}(e^{g(x)})$$

$$f'(x) = g'(x)e^{g(x)} + g(x)g'(x)e^{g(x)}$$

$$f'(x) = g'(x)e^{g(x)}(1 + g(x))$$

$$f'(2) = g'(2)e^{g(2)}(1 + g(2)) = 3e^4(1 + 4)$$

$$f'(2) = 15e^4$$

Question 12 **Answer B**

$$f(x) = \int g(x) dx \quad \Rightarrow \quad g(x) = \frac{d}{dx}(f(x)) = f'(x)$$

$$h(x) = \frac{d}{dx}(g(x)) = \frac{d}{dx}(f'(x))$$

Question 13 **Answer B**

$$n = 18, \quad \hat{p} = \frac{X}{18} \quad X \stackrel{d}{=} Bi(n = 18, p = ?)$$

$$\Pr\left(\hat{p} = \frac{1}{3}\right) = \Pr(X = 6) = \binom{18}{6} p^6 (1-p)^{12} = 0.1873$$

solving gives $p = 0.3$,

$$\Pr\left(\hat{p} < \frac{1}{2}\right) = \Pr(X < 9)$$

$$= \Pr(X \leq 8) = 0.940$$

$$\text{solve}(\text{nCr}(18,6) \cdot p^6 \cdot (1-p)^{12} = 0.1873, p) \mid 0 < p < 0.35$$

$$p = 0.3000$$

$$\text{binomCdf}(18, 0.3, 0, 8)$$

$$0.9404$$

Question 14

Answer B

If $f(x)$ is a non-zero odd function, then $f(-x) = -f(x)$

Let $f(x) = x^3$, $f(-x) = (-x)^3 = -x^3 = -f(x)$

$f \circ f(x) = f(f(x)) = f(x^3) = x^9$ which is an odd function **B.** is true.

All of **A.** **C.** and **D.** are false.

Define $f(x) = x^3$ *Done*

$f(-x) = -f(x)$ true

$f(f(-x)) = -f(f(x))$ true

Define $a(x) = f(x^2) \cdot \cos(x)$ *Done*

$a(-x) = -a(x)$ $x^6 \cdot \cos(x) = -x^6 \cdot \cos(x)$

Define $c(x) = f(x^3) \cdot \sin(x)$ *Done*

$c(-x) = -c(x)$ $x^9 \cdot \sin(x) = -x^9 \cdot \sin(x)$

Define $d(x) = f(x^2) - f(x)$ *Done*

$d(-x) = -d(x)$ $x^6 + x^3 = x^3 - x^6$

Question 15 **Answer D**

$\sum \Pr(X = x) = 1$ for all p , however since they are probabilities $0 < 1 - \frac{5p}{6} < 1 \Rightarrow 0 < p < \frac{6}{5}$

$$E(X) = \sum x \Pr(X = x) = 1 \times \frac{p}{2} + 2 \times \frac{p}{3} + 3 \left(1 - \frac{5p}{6} \right) = \frac{1}{3}(9 - 4p)$$

$$E(X^2) = \sum x^2 \Pr(X = x) = 1 \times \frac{p}{2} + 4 \times \frac{p}{3} + 9 \left(1 - \frac{5p}{6} \right) = \frac{1}{3}(27 - 17p)$$

$$\text{Var}(X) = E(X^2) - (E(X))^2 = \frac{p}{9}(21 - 16p) = \frac{1}{9}(21p - 16p^2)$$

for maximum variance $\frac{dV}{dp} = \frac{1}{9}(21 - 32p) = 0, \quad p = \frac{21}{32}$

A, B, C are all true, D is false

| A xv | B pv |
|------|-------------------|
| 1 | $p/2$ |
| 2 | $p/3$ |
| 3 | $1 - 5 \cdot p/6$ |

$$ex := \sum(xv \cdot pv) \qquad 3 - \frac{4 \cdot p}{3}$$

$$ex2 := \sum(xv^2 \cdot pv) \qquad 9 - \frac{17 \cdot p}{3}$$

$$vx := ex2 - ex^2 \qquad \frac{7 \cdot p}{3} - \frac{16 \cdot p^2}{9}$$

$$\frac{d}{dp}(vx) \qquad \frac{7}{3} - \frac{32 \cdot p}{9}$$

$$\text{solve} \left(\frac{d}{dp}(vx) = 0, p \right) \qquad p = \frac{21}{32}$$

Question 16 **Answer C**

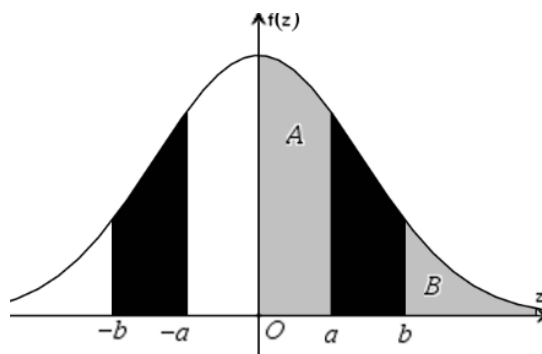
$$\Pr(-b < Z < -a \mid Z < 0)$$

$$= \frac{\Pr(-b < Z < -a)}{\Pr(Z < 0)} = \frac{\Pr(a < Z < b)}{\Pr(Z > 0)} \quad \text{since } 0 < a < b < 3$$

$$= \frac{0.5 - [\Pr(0 < Z < a) + \Pr(Z > b)]}{0.5}$$

$$= \frac{0.5 - (A + B)}{0.5}$$

$$= 1 - 2(A + B)$$



Question 17

Answer D

$$3x - 2y + z = 1$$

$$-x + y - z = 2$$

Allan stated that the general solution could be expressed as

$$x = k, \quad y = 2k - 3, \quad z = k - 5 \quad \text{for } k \in \mathbb{R}.$$

Ben stated that the general solution could be expressed as

$$x = \frac{k+3}{2}, \quad y = k, \quad z = \frac{k-7}{2} \quad \text{for } k \in \mathbb{R}.$$

Colin stated that the general solution could be expressed as

$$x = k + 5, \quad y = 2k + 7, \quad z = k \quad \text{for } k \in \mathbb{R}.$$

All of Allan, Ben and Colin are correct.

$$\text{eq1} := 3 \cdot x - 2 \cdot y + z = 1$$

$$3 \cdot x - 2 \cdot y + z = 1$$

$$\text{eq2} := -x + y - z = 2$$

$$-x + y - z = 2$$

$$\text{solve}(\text{eq1 and eq2}, \{y, z\})|x=k$$

$$y = 2 \cdot k - 3 \quad \text{and} \quad z = k - 5$$

$$\text{solve}(\text{eq1 and eq2}, \{x, z\})|y=k$$

$$x = \frac{k+3}{2} \quad \text{and} \quad z = \frac{k-7}{2}$$

$$\text{solve}(\text{eq1 and eq2}, \{x, y\})|z=k$$

$$x = k + 5 \quad \text{and} \quad y = 2 \cdot k + 7$$

Question 18

Answer D

Newton's method will succeed if the gradient is defined and non-zero at x_0 . Only **D**. has $f'(x_0) \neq 0$

$$f(x) = \sqrt{3x^2 - 7x + 2}, \quad f'(2) \text{ is not defined}$$

$$f(x) = 3x^3 - 13x^2 + 16x - 4, \quad f'(2) = 0$$

$$f(x) = (3x - 1)\log_e(x - 2), \quad f'(2) \text{ is not defined}$$

$$f(x) = (3x - 1)e^{x-2}, \quad f'(2) \neq 0$$

| | |
|--|------|
| Define $f_a(x) = \sqrt{3 \cdot x^2 - 7 \cdot x + 2}$ | Done |
|--|------|

| | |
|-------------------------------|-------|
| $\frac{d}{dx}(f_a(x)) _{x=2}$ | undef |
|-------------------------------|-------|

| | |
|---|------|
| Define $f_b(x) = 3 \cdot x^3 - 13 \cdot x^2 + 16 \cdot x - 4$ | Done |
|---|------|

| | |
|-------------------------------|---|
| $\frac{d}{dx}(f_b(x)) _{x=2}$ | 0 |
|-------------------------------|---|

| | |
|--|------|
| Define $f_c(x) = (3 \cdot x - 1) \cdot \ln(x - 2)$ | Done |
|--|------|

| | |
|-------------------------------|-------|
| $\frac{d}{dx}(f_c(x)) _{x=2}$ | undef |
|-------------------------------|-------|

| | |
|---|------|
| Define $f_d(x) = (3 \cdot x - 1) \cdot e^{x-2}$ | Done |
|---|------|

| | |
|-------------------------------|---|
| $\frac{d}{dx}(f_d(x)) _{x=2}$ | 8 |
|-------------------------------|---|

Question 19

Answer C

| iterations | x_{left} | x_{mid} | x_{right} | $f(x_{left}) \cdot f(x_{mid})$ |
|------------|------------|-----------|-------------|--------------------------------|
| 0 | 2 | 2.5 | 3 | -1.25 |
| 1 | 2 | 2.25 | 2.5 | -0.0625 |
| 2 | 2 | 2.125 | 2.25 | 0.4844 |
| 3 | 2.125 | 2.1875 | 2.25 | 0.1041 |

```
xleft  xmid  xright  f(xleft)*f(xmid)
2.0000 2.5000 3.0000  -1.2500
2.0000 2.2500 2.5000  -0.0625
2.0000 2.1250 2.2500  0.4844
2.1250 2.1875 2.2500  0.1041
```

```
Define bisection()=
Prgm
maxiter:=4
xleft:=2
xright:=3
Define f(x)=x^2-5
If f(xleft)*f(xright)>0 Then
  Disp "starting values will not converge"
  Return
EndIf
i:=0
Disp " xleft  xmid  xright  f(xleft)*f(xmid)"
While i<maxiter
  xmid:=(xleft+xright)/2
  Disp xleft,xmid,xright," " f(xleft)*f(xmid)
  If f(xleft)*f(xmid)<0 Then
    xright:=xmid
  Else
    xleft:=xmid
  EndIf
  i:=i+1
EndWhile
EndPrgm
```

Question 20

Answer A

$$\sin^2(x) = \frac{a}{c}, \quad \sin(x) = \sqrt{\frac{a}{c}}, \quad \cos^2(y) = \frac{b}{c}, \quad \cos(y) = \sqrt{\frac{b}{c}}$$

since $0 < a < b < c < 1$, $\sin(x) > 0$ and $\cos(y) > 0$

$$\begin{aligned} & \log_2(\sin(x)\cos(y)) \\ &= \log_2\left(\sqrt{\frac{a}{c}}\sqrt{\frac{b}{c}}\right) = \log_2\left(\frac{\sqrt{ab}}{c}\right) = \log_2(\sqrt{ab}) - \log_2(c) \\ &= \log_e\left((ab)^{\frac{1}{2}}\right) - \log_2(c) = \frac{1}{2}(\log_2(ab)) - \log_2(c) \\ &= \frac{1}{2}(\log_2(a) + \log_2(b)) - \log_2(c) \end{aligned}$$

END OF SECTION A SUGGESTED ANSWERS

SECTION B

Question 1

a. $f : R \rightarrow R, f(x) = x^4 - 4x^3 + 3$

$m(x) = f'(x) = 4x^2(x-3) = 0$

for turning points

$x = 0, x = 3, f(3) = -24$

$(3, -24)$ is an absolute minimum turning point

A1

b. $m'(x) = 12x^2 - 24x$

$m'(x) = 12x(x-2) = 0$ for inflection points

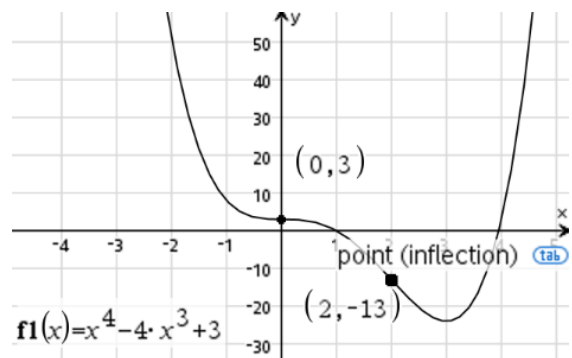
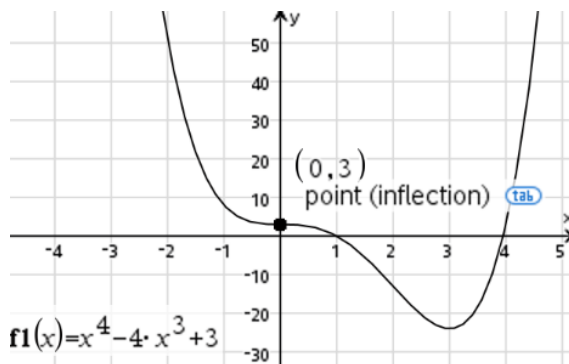
$x = 0, 2$

$f(0) = 3, f(2) = -13$

$(0, 3)$ is a stationary point of inflection

$(2, -13)$ is a point of inflexion

A1



c. at $x = 2, f(2) = -13, f'(2) = -16$

the tangent line at $x = 2$ is

$y + 13 = -16(x - 2) = -16x + 32$

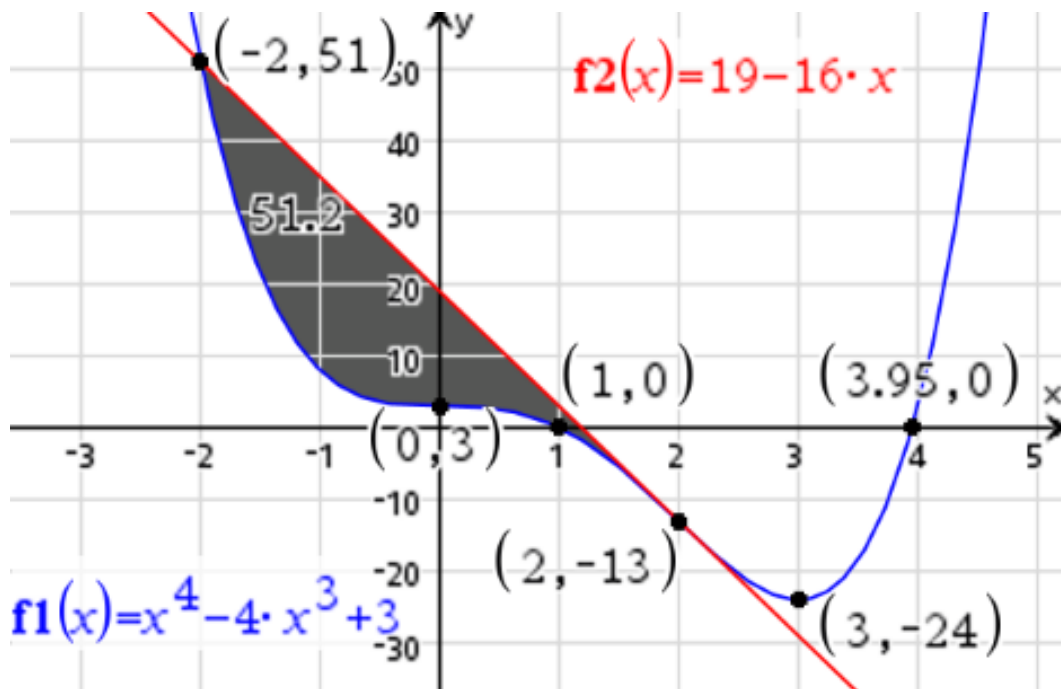
$y = g(x) = -16x + 19$

note the curve crosses the tangent at the point of inflection.

A1

d.

G2



e. $g(x) - f(x)$

$$= (-16x + 19) - (x^4 - 4x^3 + 3)$$

$$= -x^4 + 4x^3 - 16x + 16$$

M1

$$= -(x+2)(x-2)^3 = (x+2)(2-x)^3$$

$$g(x) = f(x), \Rightarrow x = \pm 2$$

i. the area is $A = \int_{-b}^b (g(x) - f(x)) dx$

$$A = \int_{-2}^2 (x+2)(2-x)^3 dx$$

A1

$$b = 2, n = 3$$

ii. $A = \frac{256}{5} = 51\frac{1}{5} = 51.2$

A1

f. solving $\frac{f(c) - f(1)}{c - 1} = -12, c > 1$ gives $c = \sqrt{3}$ or $c = 3$

A1

g. $h: \mathbb{R} \rightarrow \mathbb{R}, h(x) = f(x) + k$, need to translate the graph up by 24 or more units, so that for the graph to not cross the x -axis, require $k > 24$ or $k \in (24, \infty)$

A1

$$\text{Define } f1(x) = x^4 - 4 \cdot x^3 + 3 \quad \text{Done}$$

$$\text{factor}(f1(x)) \quad (x-1) \cdot (x^3 - 3 \cdot x^2 - 3 \cdot x - 3)$$

$$\text{solve}(f1(x)=0, x) \quad x=1.00000 \text{ or } x=3.95137$$

$$\text{solve}\left(\frac{d}{dx}(f1(x))=0, x\right) \quad x=0 \text{ or } x=3$$

$$f1(3) \quad -24$$

$$f1(2) \quad -13$$

$$\text{tangentLine}(f1(x), x, 2) \quad 19 - 16 \cdot x$$

$$\text{Define } f2(x) = 19 - 16 \cdot x \quad \text{Done}$$

$$\text{solve}(f1(x)=f2(x), x) \quad x=-2 \text{ or } x=2$$

$$f2(x) - f1(x) \quad -x^4 + 4 \cdot x^3 - 16 \cdot x + 16$$

$$\text{factor}(f2(x) - f1(x)) \quad -(x-2)^3 \cdot (x+2)$$

$$\int_{-2}^2 \left(-(x-2)^3 \cdot (x+2) \right) dx \quad 51.20000$$

$$\text{solve}\left(\frac{f1(c) - f1(1)}{c-1} = -12, c\right) | c > 1 \quad c = \sqrt{3} \text{ or } c = 3$$

Question 2 $f : R \rightarrow R, f(x) = e^{-x^2}$

a.i. $A(a) = 2af(a) = 2ae^{-a^2}$

$$\frac{dA}{da} = (2 - 4a^2)e^{-a^2} = 0 \text{ for maximum area } a = \frac{\sqrt{2}}{2} \quad \text{M1}$$

ii. $A_{\max} = A\left(\frac{\sqrt{2}}{2}\right) = \sqrt{\frac{2}{e}}$ A1

iii. the inflexion points are $(\pm 0.7071, 0.6065)$ $a = \frac{\sqrt{2}}{2} \approx 0.7071$
yes Jenny's assertion is correct. A1

b.i. $s(a) = \sqrt{a^2 + (f(a))^2} = \sqrt{a^2 + e^{-2a^2}}$
 $\frac{ds}{da} = 0$ for minimum area $a = \frac{1}{2}\sqrt{\log_e(4)}$ A1

ii. $s_{\min} = s\left(\frac{1}{2}\sqrt{\log_e(4)}\right) = \frac{1}{2}\sqrt{\log_e(4) + 2}$ A1

c. $f(x) = e^{-x^2} \rightarrow f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} = \frac{1}{\sigma\sqrt{2\pi}} e^{-\left(\frac{x-\mu}{\sqrt{2}\sigma}\right)^2}$ A1

$x = \frac{x' - \mu}{\sqrt{2}\sigma}, x' = \sqrt{2}\sigma x + \mu, \mu > 0$ A2

- dilate by a factor of $\frac{1}{\sigma\sqrt{2\pi}}$ parallel to the y -axis (or away from the x -axis)
- dilate by a factor of $\sqrt{2}\sigma$ parallel to the x -axis (or away from the y -axis)
- translate by a factor of μ to the right parallel to the x -axis (or away from the y -axis)

Define $f1(x) = e^{-x^2}$ Done

Define $r(a) = 2 \cdot a \cdot f1(a)$ Done

$\frac{d}{da}(r(a))$ $(2 - 4 \cdot a^2) \cdot e^{-a^2}$

solve $\left(\frac{d}{da}(r(a)) = 0, a\right) | a > 0$ $a = \frac{\sqrt{2}}{2}$

$r\left(\frac{\sqrt{2}}{2}\right)$ $\frac{-1}{e^{\frac{1}{2}}} \cdot \sqrt{2}$

$\frac{d^2}{dx^2}(f1(x))$ $(4 \cdot x^2 - 2) \cdot e^{-x^2}$

solve $\left(\frac{d^2}{dx^2}(f1(x)) = 0, x\right)$ $x = \frac{-\sqrt{2}}{2}$ or $x = \frac{\sqrt{2}}{2}$

Define $s(a) = \sqrt{a^2 + (f1(a))^2}$ Done

solve $\left(\frac{d}{da}(s(a)) = 0, a\right) | a > 0$ $a = \frac{\sqrt{2 \cdot \ln(2)}}{2}$

$s\left(\frac{\sqrt{2 \cdot \ln(2)}}{2}\right)$ $\frac{\sqrt{2 \cdot (\ln(2) + 1)}}{2}$

Question 3

a.i. $P \stackrel{d}{=} Bi(n = 50, p = 0.46)$

| | |
|--------------------------------------|----------|
| <code>binomCdf(50,0.46,26,50)</code> | 0.238643 |
|--------------------------------------|----------|

$$\Pr(P > 25)$$

$$= \Pr(26 \leq P \leq 50) = 0.2386$$

A1

ii. $E \stackrel{d}{=} Bi(n = ?, p = 0.07)$

$$\Pr(E \geq 2) \geq 0.3$$

$$1 - \Pr(E \leq 1) \leq 0.7$$

$$1 - (\Pr(E = 0) + \Pr(E = 1)) \leq 0.7$$

$$\Pr(E = 0) + \Pr(E = 1) \geq 0.3$$

$$0.93^n + n \times 0.93^{n-1} \times 0.07 \geq 0.3$$

$$n = 16$$

| | |
|--|---------------|
| <code>solve((0.93)^n + n * (0.03)^(n-1) * 0.07 = 0.31, n)</code> | $n = 16.1385$ |
|--|---------------|

| | |
|--|--------|
| <code>binomCdf(n,0.07,2,n) n=15</code> | 0.2832 |
|--|--------|

| | |
|--|--------|
| <code>binomCdf(n,0.07,2,n) n=16</code> | 0.3098 |
|--|--------|

| | |
|--------------------------------------|--|
| <code>invBinomN(0.7,0.07,1,1)</code> | $\begin{bmatrix} 15 & 0.7168 \\ 16 & 0.6902 \end{bmatrix}$ |
|--------------------------------------|--|

A1

b. $\Pr(EH | NB) = \frac{\Pr(EH \cap NB)}{\Pr(NB)} = \frac{23}{177}$

$$= \frac{0.23(1-b)}{0.23(1-b) + 0.77 \times 0.6} = \frac{23}{177}$$

M1

$$b = 0.7, \quad 70\%$$

A1

c.i. $B \stackrel{d}{=} N(96, 8^2)$ time in months

$$\Pr(B > 120 | B \geq 108)$$

M1

$$= \frac{\Pr(B > 120)}{\Pr(B \geq 108)} = \frac{0.00135}{0.0668}$$

| | |
|----------------------------------|--------|
| <code>normCdf(120,∞,96,8)</code> | 0.0202 |
| <code>normCdf(108,∞,96,8)</code> | |

$$= 0.0202$$

A1

ii. $\Pr(B > t) = 0.8$

$$\frac{t-96}{8} = 0.8416$$

$$t = 102.73 \text{ months}$$

$$8.56 \text{ years}$$

| | |
|--------------------------------|--------|
| <code>invNorm(0.8,96,8)</code> | 8.5611 |
| 12 | |

A1

iii. $S \stackrel{d}{=} Bi(n = 10, p = 0.0668)$

$$\Pr(S > 2)$$

$$= \Pr(3 \leq S \leq 10) = 0.0251$$

| | |
|-------------------------------------|--------|
| <code>p:=normCdf(108,∞,96,8)</code> | 0.0668 |
|-------------------------------------|--------|

A1

| | |
|----------------------------------|--------|
| <code>binomCdf(10,p,3,10)</code> | 0.0251 |
|----------------------------------|--------|

A1

d. White: $\hat{p}_W = 0.34$, 95%, $z = 1.96$

$$(1) CL_W = 0.34 - 1.96 \sqrt{\frac{0.34(1-0.34)}{n_W}}$$

Black: $\hat{p}_B = 0.21$, 99%, $z = 2.576$

$$(2) CU_B = 0.21 + 2.576 \sqrt{\frac{0.21(1-0.21)}{n_B}}$$

solving (1) = (2) $CL_W = CU_B$ with $n_B = 3n_W$

gives $n_W = 139$

$$z_{95} = \text{invNorm}(0.975, 0, 1) \quad 1.9600$$

$$z_{99} = \text{invNorm}(0.995, 0, 1) \quad 2.5758$$

$$clw = 0.34 - z_{95} \cdot \sqrt{\frac{0.34 \cdot (1-0.34)}{nw}}$$

$$0.3400 - 0.9285 \cdot \sqrt{\frac{1}{nw}}$$

$$clu = 0.21 + z_{99} \cdot \sqrt{\frac{0.21 \cdot (1-0.21)}{nb}}$$

$$1.0492 \cdot \sqrt{\frac{1}{nb}} + 0.2100$$

$$\text{solve}(clw = clu, nw) | nb = 3 \cdot nw \quad nw = 139.2732$$

M1

A1

A1

e. $T \stackrel{d}{=} N(\mu = ?, \sigma^2 = ?)$ time in years

$$\Pr(T > 7) = 0.86$$

$$\Pr(T < 7) = 0.14$$

$$(1) \frac{7 - \mu}{\sigma} = -1.0803$$

$$\Pr(T < 5) = 0.05$$

$$(2) \frac{5 - \mu}{\sigma} = -1.6449$$

solving (1), (2) $\mu = 10.8$, $\sigma = 3.5$

$$\text{invNorm}(0.14, 0, 1) \quad -1.0803$$

$$\text{invNorm}(0.05, 0, 1) \quad -1.6449$$

M1

$$\text{solve}\left(\frac{7-m}{s} = -1.0803 \text{ and } \frac{5-m}{s} = -1.6449, \{m, s\}\right)$$

$$s = 3.5423 \text{ and } m = 10.8268$$

A1

$$f. f(t) = \begin{cases} b(2t-1) & \text{for } \frac{1}{2} \leq t \leq 1 \\ \frac{b}{\left(t - \frac{1}{2}\right)^2} & \text{for } 1 < t \leq 4 \\ 0 & \text{elsewhere} \end{cases}$$

since it is a probability density function $\int_{0.5}^4 f(t) dt = 1$ solving gives $b = \frac{28}{55}$

$$E(T) = \int_{0.5}^4 t f(t) dt = 1.5331$$

$$E(T^2) = \int_{0.5}^4 t^2 f(t) dt = 2.8263$$

$$sd(T) = \sqrt{E(T^2) - (E(T))^2} = 0.6899$$

M1

$$E(T) + 2sd(T) = 2.9129$$

$$E(T) - 2sd(T) = 0.1533 < 0.5$$

$$\Pr(0.5 \leq T \leq E(T) + 2sd(T))$$

$$= \Pr(0.5 \leq T \leq 2.9129)$$

$$= \int_{0.5}^{2.9129} f(t) dt = 0.9345$$

A1

$$\text{Define } f(t) = \begin{cases} b \cdot (2 \cdot t - 1), & \frac{1}{2} \leq t < 1 \\ \frac{b}{\left(t - \frac{1}{2}\right)^2}, & 1 \leq t \leq 4 \end{cases} \quad \text{Done}$$

$$\text{ex} := \int_{\frac{1}{2}}^4 (t \cdot f(t)) dt \quad 1.5331$$

$$\text{solve} \left(\int_{\frac{1}{2}}^4 f(t) dt = 1, b \right) \quad b = \frac{28}{55}$$

$$\text{ex2} := \int_{\frac{1}{2}}^4 (t^2 \cdot f(t)) dt \quad 2.8263$$

$$\text{Define } f(t) = \begin{cases} b \cdot (2 \cdot t - 1), & \frac{1}{2} \leq t < 1 \\ \frac{b}{\left(t - \frac{1}{2}\right)^2}, & 1 \leq t \leq 4 \end{cases} \quad | b = \frac{28}{55} \quad \text{Done}$$

$$sdx := \sqrt{\text{ex2} - \text{ex}^2} \quad 0.6899$$

$$\text{ex} + 2 \cdot sdx \quad 2.9129$$

$$\text{ex} - 2 \cdot sdx \quad 0.1533$$

$$\int_{\frac{1}{2}}^{2.91285} f(t) dt \quad 0.9345$$

Question 4

a. $f : [-\pi, \pi] \rightarrow \mathbb{R}, f(x) = x^2 \cos(x)$

$$f(-x) = (-x)^2 \cos(-x)$$

$$= x^2 \cos(x) = f(x)$$

A1

so f is an even function and the graph of $y = f(x)$

is symmetrical about the y -axis.

A1

b. $f'(x) = 2x \cos(x) - x^2 \sin(x) = x(2 \cos(x) - x \sin(x))$

for non-zero turning points $g(x) = 2 \cos(x) - x \sin(x) = 0$

$$g'(x) = -3 \sin(x) - x \cos(x), \quad x_0 = 0.75$$

$$x_1 = x_0 - \frac{g(x_0)}{g'(x_0)} = 1.117$$

M1

$$x_2 = x_1 - \frac{g(x_1)}{g'(x_1)} = 1.077$$

A1

| | |
|-------|-------|
| x_0 | 0.75 |
| x_1 | 1.117 |
| x_2 | 1.077 |

| | |
|------------------------------------|---|
| Define $f(x) = x^2 \cdot \cos(x)$ | Done |
| Define $m(x) = \frac{d}{dx}(f(x))$ | Done |
| $m(x)$ | $2 \cdot x \cdot \cos(x) - x^2 \cdot \sin(x)$ |
| Define $g(x) = \frac{m(x)}{x}$ | Done |
| $g(x)$ | $2 \cdot \cos(x) - x \cdot \sin(x)$ |

| | |
|--------------------------------------|--------------------------------------|
| Define $dg(x) = \frac{d}{dx}(g(x))$ | Done |
| $dg(x)$ | $-x \cdot \cos(x) - 3 \cdot \sin(x)$ |
| $0.75 - \frac{g(0.75)}{dg(0.75)}$ | 1.117 |
| $1.117 - \frac{g(1.117)}{dg(1.117)}$ | 1.077 |

c.i. $y - a^2 \cos(a) = (2a \cos(a) - a^2 \sin(a))(x - a)$

$$y = (2a \cos(a) - a^2 \sin(a))x - a^2 (\cos(a) - a \sin(a))$$

A1

ii. solving $y = 0$ when $x = \pi$ and $0 < a < \pi$ gives $a = 1.151$, and

A1

$$y = 0.852 - 0.271x$$

A1

tangentLine($f(x), x, a$)

$$2.000 \cdot a \cdot (\cos(a) - 0.500 \cdot a \cdot \sin(a)) \cdot x - a^2 \cdot (\cos(a) - a \cdot \sin(a))$$

$$\text{solve}(a \cdot (2 \cdot \cos(a) - a \cdot \sin(a)) \cdot x - a^2 \cdot (\cos(a) - a \cdot \sin(a)) = 0, a) | x = \pi$$

$$(a - 2 \cdot \pi) \cdot \cos(a) - a \cdot (a - \pi) \cdot \sin(a) = 0 \text{ and } 0 < a < \pi$$

$$a \cdot (2 \cdot \cos(a) - a \cdot \sin(a)) \cdot x - a^2 \cdot (\cos(a) - a \cdot \sin(a)) | a = 1.1509284$$

$$0.852 - 0.271 \cdot x$$

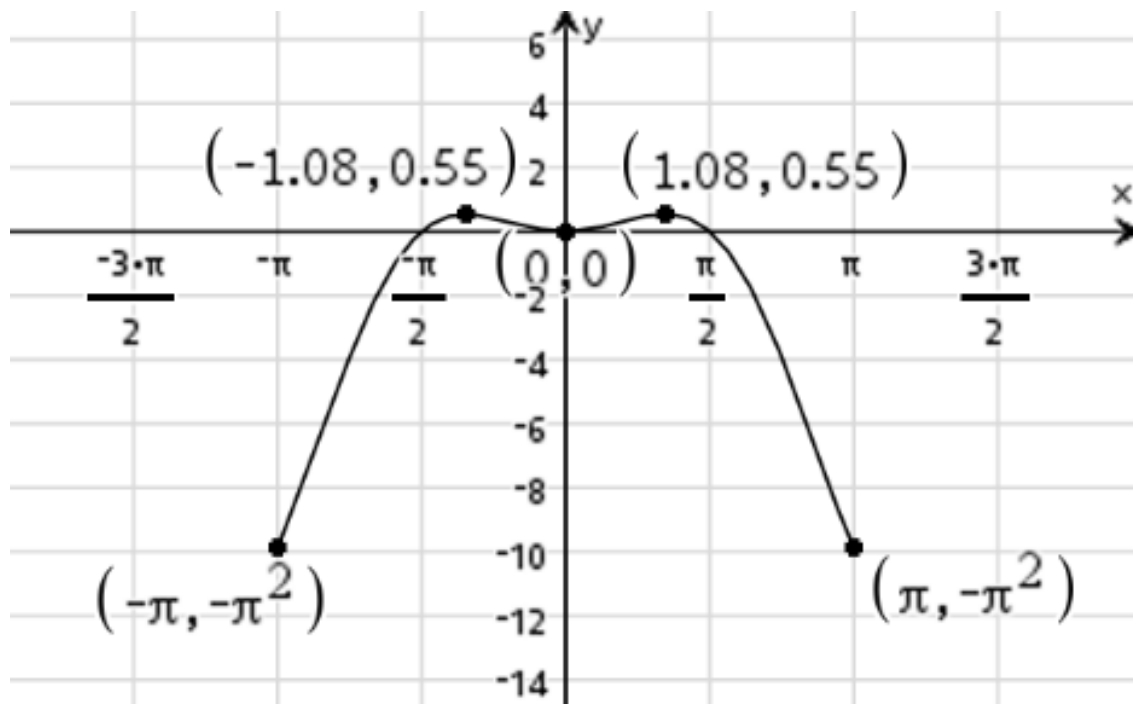
d. endpoints $(\pm\pi, -\pi^2)$

local minimum turning point $(0, 0)$

A1

absolute maximum turning points $(\pm 1.08, 0.55)$

G2



e. f is strictly increasing for $x \in [-3.14, -1.08]$ or $x \in [0, 1.08]$

A1

f.
$$\bar{f} = \frac{1}{\pi - (-\pi)} \int_{-\pi}^{\pi} x^2 \cos(x) dx = -2$$

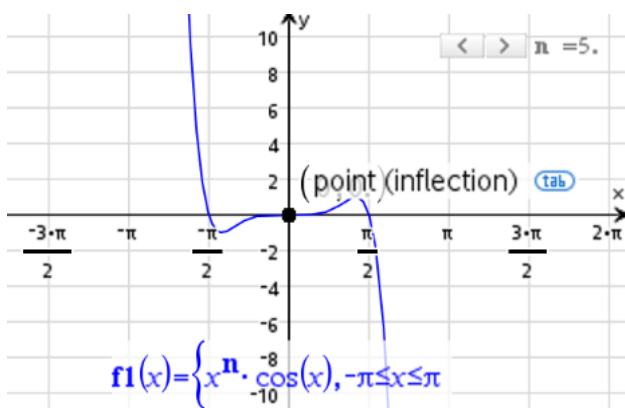
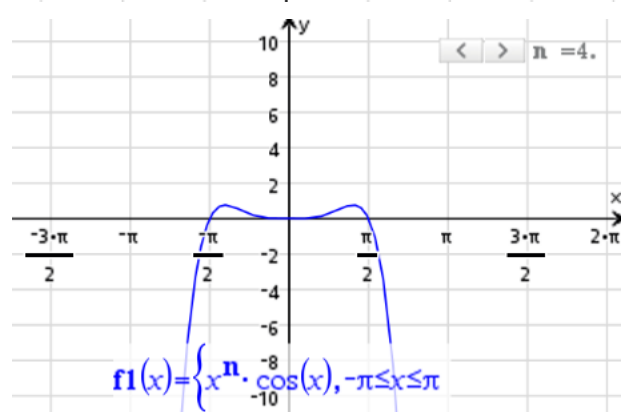
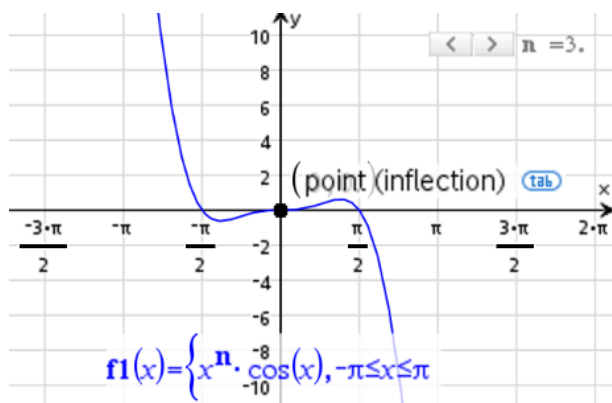
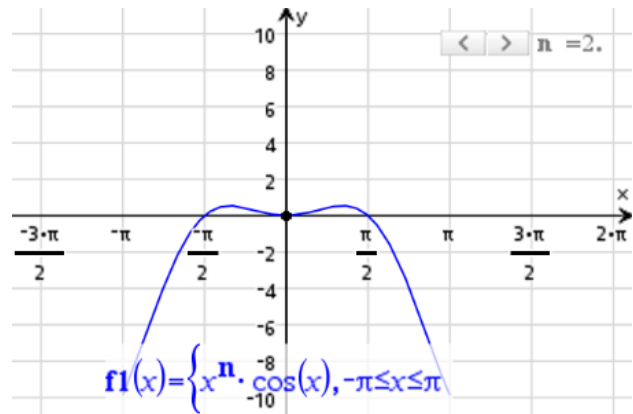
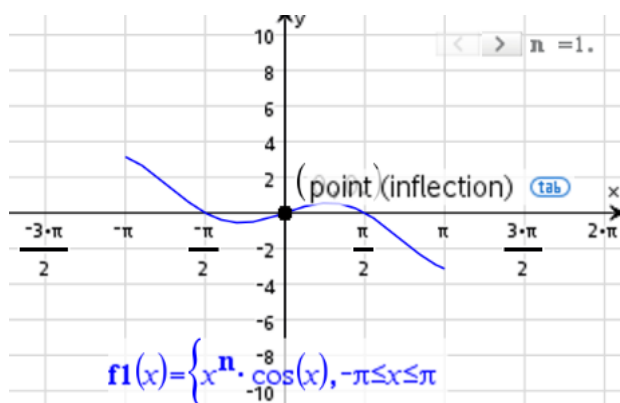
A1

$$\frac{1}{\pi - (-\pi)} \int_{-\pi}^{\pi} f(x) dx = -2$$

g. $f_n : [-\pi, \pi] \rightarrow \mathbb{R}$, $f_n(x) = x^n \cos(x)$, $n \in \mathbb{N}$.

A2

| values of n | The graph of $y = f_n(x)$ at the origin has |
|--|---|
| $n = 1$ | a point of inflection |
| n even, $2, 4, 6, \dots$ $n = 2k, k \in \mathbb{Z}^+$ | a local minimum turning point |
| n odd, $3, 5, 7, \dots$ $n = 2k + 1, k \in \mathbb{Z}^+$ | a stationary point of inflection |



Question 5

a. $f : \left[\frac{3}{2}, \infty\right) \rightarrow R, f(x) = \sqrt{4x^2 - 9}$

$f: y = \sqrt{4x^2 - 9}$

$f^{-1}: x = \sqrt{4y^2 - 9}, x^2 = 4y^2 - 9, y^2 = \frac{x^2 + 9}{4}$

domain $f =$ range of $f^{-1} = \left[\frac{3}{2}, \infty\right)$

domain $f^{-1} =$ range of $f = [0, \infty)$

$f^{-1}: [0, \infty) \rightarrow R, f^{-1}(x) = \frac{\sqrt{x^2 + 9}}{2}$

A1

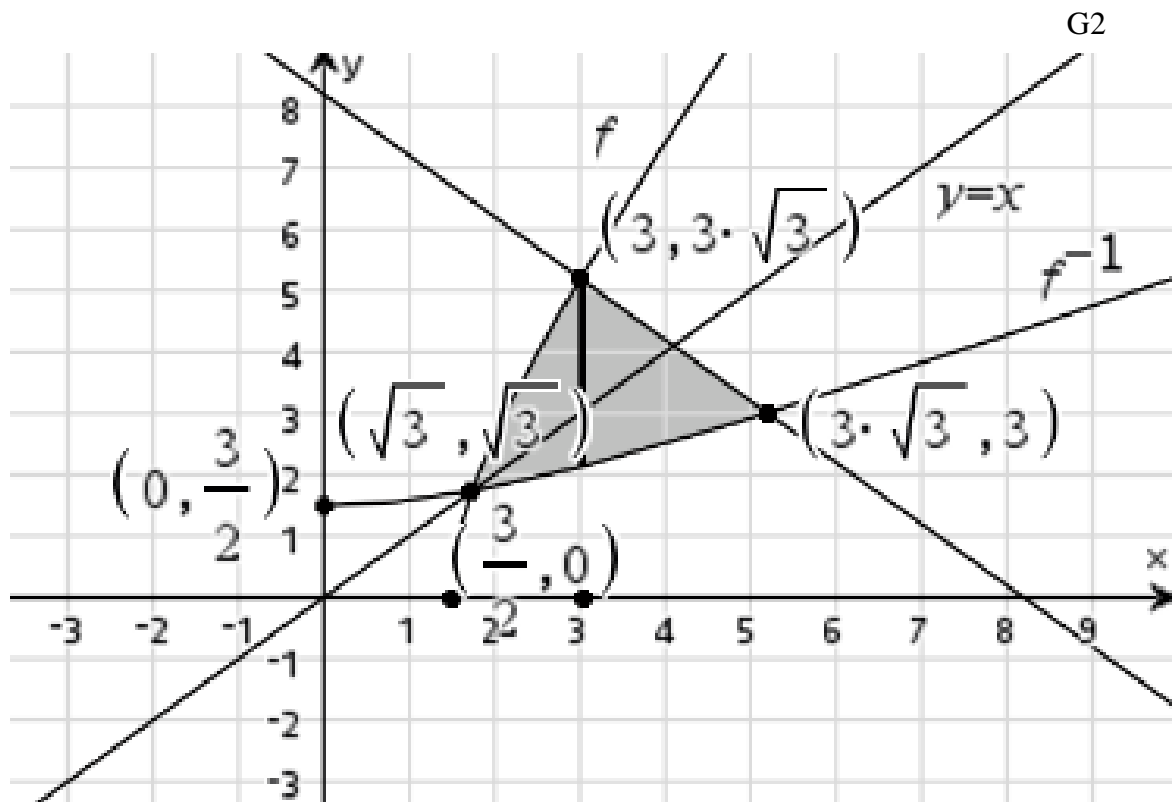
b. solving $f(x) = f^{-1}(x) \Rightarrow x = \sqrt{3}$

$P(\sqrt{3}, \sqrt{3})$

A1

| | | |
|---|--|----------------|
| Define $f1(x) = \sqrt{4 \cdot x^2 - 9}$ | Done solve($f1(x) = f2(x), x x > 0$) | $x = \sqrt{3}$ |
| Define $f2(x) = \frac{\sqrt{x^2 + 9}}{2}$ | Done | |

c.



- d.i.** The line $y = -x + 3(\sqrt{3} + 1)$ intersects the graph of $f(x) = \sqrt{4x^2 - 9}$ at the point $(3, 3\sqrt{3})$ and the line $y = -x + 3(\sqrt{3} + 1)$ intersects the graph of $f^{-1}(x) = \frac{\sqrt{x^2 + 9}}{2}$ at the point $(3\sqrt{3}, 3)$.

The area is $A = \int_{\sqrt{3}}^3 (f(x) - f^{-1}(x)) dx + \int_3^{3\sqrt{3}} (-x + 3(\sqrt{3} + 1) - f^{-1}(x)) dx$ M1

$$A = \int_{\sqrt{3}}^3 \left(\sqrt{4x^2 - 9} - \frac{\sqrt{x^2 + 9}}{2} \right) dx + \int_3^{3\sqrt{3}} \left(-x + 3(\sqrt{3} + 1) - \frac{\sqrt{x^2 + 9}}{2} \right) dx$$
 A1

$$\int_{\sqrt{3}}^3 (f1(x) - f2(x)) dx + \int_3^{3 \cdot \sqrt{3}} (f4(x) - f2(x)) dx$$

5.5456

ii. $A = 5.546$ A1

e. $f(x) = \sqrt{4x^2 - 9}$ $\frac{d}{dx}(f1(x))|_{x=\sqrt{3}}$
4

$f'(x) = \frac{4x}{\sqrt{4x^2 - 9}}$ $\frac{d}{dx}(f2(x))|_{x=\sqrt{3}}$
 $\frac{1}{4}$

$f'(\sqrt{3}) = 4 = \tan(\theta_1)$ $\tan^{-1}(4) - \tan^{-1}\left(\frac{1}{4}\right)$
61.9275

$f^{-1}(x) = \frac{\sqrt{x^2 + 9}}{2}$

$\frac{d}{dx}(f^{-1}(x)) = \frac{x}{\sqrt{x^2 + 9}}$ A1

$\frac{d}{dx}(f^{-1}(x)) \Big|_{x=\sqrt{3}} = \frac{1}{4} = \tan(\theta_2)$

$\theta_1 - \theta_2 = \tan^{-1}(4) - \tan^{-1}\left(\frac{1}{4}\right) = 61.9^\circ$ A1

f. $f(x) = \sqrt{kx^2 - 9}$ $x \in \left[\frac{3}{\sqrt{k}}, \infty \right)$
 domain $f = \left[\frac{3}{\sqrt{k}}, \infty \right)$ since it is a one-one
 increasing function, so $k > 0$.
 $f^{-1}(x) = \sqrt{\frac{x^2 + 9}{k}}$

Define $f(x) = \sqrt{kx^2 - 9}$ Done

Define $g(x) = \frac{\sqrt{x^2 + 9}}{\sqrt{k}}$ Done

solve($f(x) = g(x), x$)
 $x = \frac{3}{\sqrt{k-1}}$ and $\frac{1}{k-1} \geq 0$ or $x = \frac{-3}{\sqrt{k-1}}$ and $\frac{1}{k-1}$

The graphs do not intersect when $0 < k \leq 1$ or $k \in (0, 1]$

A1

g. $f(x) = \sqrt{kx^2 - 9}$, $f'(x) = \frac{kx}{\sqrt{kx^2 - 9}}$, $f'(c) = \frac{kc}{\sqrt{kc^2 - 9}} = \tan(\theta_1)$
 $f^{-1}(x) = \sqrt{\frac{x^2 + 9}{k}}$, $\frac{d}{dx}(f^{-1}(x)) = \frac{x}{\sqrt{k(x^2 + 9)}}$, $\frac{d}{dx}(f^{-1}(x)) \Big|_{x=c} = \frac{c}{\sqrt{k(c^2 + 9)}} = \tan(\theta_2)$

$f(c) = f^{-1}(c)$

A1

$\Rightarrow k = \frac{c^2 + 9}{c^2}$, $c = \frac{3}{\sqrt{k-1}}$

$\tan^{-1}(5) - \tan^{-1}\left(\frac{1}{5}\right)$ 67.3801

$\theta_1 - \theta_2 = \tan^{-1}\left(\frac{12}{5}\right) = \tan^{-1}(5) - \tan^{-1}\left(\frac{1}{5}\right)$

$\tan^{-1}\left(\frac{12}{5}\right)$ 67.3801

solving $\frac{kc}{\sqrt{kc^2 - 9}} = 5$ and $\frac{c}{\sqrt{k(c^2 + 9)}} = \frac{1}{5}$

eq1: $\frac{c \cdot k}{\sqrt{c^2 \cdot k - 9}} = 5$ $\frac{c \cdot k}{\sqrt{c^2 \cdot k - 9}} = 5$

with $c = \frac{3}{\sqrt{k-1}}$

eq2: $\frac{c}{\sqrt{(c^2 + 9) \cdot k}} = \frac{1}{5}$ $\frac{c}{\sqrt{(c^2 + 9) \cdot k}} = \frac{1}{5}$

gives $c = \frac{3}{2}$

$k = 5$

Δ solve(eq1 and eq2, k) | $c = \frac{3}{\sqrt{k-1}}$ $k=5$

A1

END OF SECTION B SUGGESTED ANSWERS

End of detailed answers for the
2024 Kilbaha VCE Mathematical Methods Trial Examination 2

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